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Effect of water-wall interaction potential on the properties of nanoconfined water

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Much of the understanding of bulk liquids has progressed through study of the limiting case in which molecules interact via purely repulsive forces, such as a hard-core or “repulsive ramp” potential. In the same spirit, we report progress on the understanding of confined water by examining the behavior of waterlike molecules interacting with planar walls via purely repulsive forces and compare our results with those obtained for Lennard-Jones (LJ) interactions between the molecules and the walls. Specifically, we perform molecular dynamics simulations of 512 waterlike molecules interacting via the TIP4P potential and confined between two smooth planar walls that are separated by 1.1 nm. At this separation, there are either two or three molecular layers of water, depending on density. We study two different forms of repulsive confinement, when the water-wall interaction potential is either (i) $1/r^9$ or (ii) a WCA-like repulsive potential. We find that the thermodynamic, dynamic, and structural properties of the liquid in purely repulsive confinements qualitatively match those for a system with a pure LJ attraction to the wall. In previous studies that include attractions, freezing into monolayer or trilayer ice was seen for this wall separation. Using the same separation as these previous studies, we find that the crystal state is not stable with $1/r^9$ repulsive walls but is stable with WCA-like repulsive confinement. However, by carefully adjusting the separation of the plates with $1/r^9$ repulsive interactions so that the effective space available to the molecules is the same as that for LJ confinement, we find that the same crystal phases are stable. This result emphasizes the importance of comparing systems only using the same effective confinement, which may differ from the geometric separation of the confining surfaces.

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I. INTRODUCTION

Confinement of water in nanopores affects many properties of water, such as freezing temperature, crystal structure [1–7], the glass transition temperature, and the position of the hypothesized liquid-liquid (LL) critical point [8–19]. Indeed, water confined in nanoscale geometries has received much recent attention, in part because of its importance in biology, engineering, geophysics, and atmospheric sciences. The effects of different kinds of confinement have been studied, both using experiments and simulations [3,4,7,20–27].

Bulk supercooled water—water cooled below the equilibrium freezing temperature—shows many anomalous properties [2,8,28–30]. Experiments find that at low temperatures, various response functions, such as isothermal compressibility and specific heat, increase sharply. There has been comparatively less research on confined water. Using the ST2 potential to model water confined between smooth plates [31], a LL phase transition has been proposed for confined water. A liquid-to-amorphous transition is seen in simulations of water using the TIP4P potential [32] confined in carbon nanotubes [4]. Recent theoretical work [33] suggests that hydrophobic Lennard-Jones (LJ) confinement shifts the LL transition to lower temperature and lower pressure compared to bulk water, a feature also suggested by simulations of water confined between hydrophobic plates [24].

Confinement is known to enhance solidification of molecules that are more or less spherical [34–36]. However, careful experiments on thin films of water show that water performs extremely well as a lubricant, suggesting that confined water may be more fluid than bulk water [37]. Recent experiments show that water in hydrophilic confinement, when cooled to very low $T$, does not freeze [13]—a phenomenon also supported by simulation studies [38,39]. In contrast, simulations [3,4,7,23–25] show that hydrophobically confined water does freeze into different crystalline structures, which do not have counterparts in bulk water. Indeed monolayer, bilayer, and trilayer ice have all been found in simulations [3,4,7,23–25]. Thus hydrophobic confinement seems to facilitate the freezing of water. However, the reason for this facilitation is not yet fully understood. The hydrogen-bond interaction between water molecules is an order of magnitude stronger than Van der Waals attraction with the hydrophobic walls. Thus one may hypothesize that freezing in hydrophobic confinement depends critically on the separation between confining walls that may distort or facilitate a particular crystalline structure, rather than on the weak details of the water-wall interaction potential. To test this hypothesis we perform molecular dynamics (MD) simulations of water in two different forms of repulsive confinement. Specifically, we study:

1. The $1/r^9$ repulsive part of the LJ potential studied in Ref. [24].
2. The same potential used in Ref. [24] but truncated and shifted such that there is no attractive part in the potential, analogous to the Weeks-Chandler-Anderson (WCA-like) potential [40]. This potential allows us to examine the role, if any, the attractive part of the water-wall LJ potential plays in determining the thermodynamics and structure of confined water, much as studying the repulsive ramp potential [41].
allows us to examine the role of the attractive part of the Jagla potential with an attractive well [42].

We compare the case when the water-wall interactions are purely repulsive ("repulsive confinement") with the studied case of pure LJ confinement [24]. We also compare the freezing in repulsive confinements with the freezing found when the water-wall interactions are represented by an LJ interaction ("LJ hydrophobic confinement") [3,24].

This paper is organized as follows: In Sec. II, we provide details of our simulations and analysis methods. Simulation results for the liquid state are provided in Sec. III. In Sec. IV we discuss the freezing properties of the systems we studied.

II. SIMULATION AND ANALYSIS METHODS

We perform MD simulations of a system composed of waterlike molecules confined between two smooth walls. The molecules interact via the TIP5P pair potential [43] which, like the ST2 [44] potential, treats each water molecule as a tetrahedral, rigid, and nonpolarizable unit consisting of five point sites [45]. The TIP5P potential predicts many of the anomalies of bulk water [46]. For example, TIP5P reproduces the density anomaly at \( T = 277 \) K and \( P = 1 \) atm and its structural properties compare well with experiments [43,46–50]. TIP5P is known to crystallize at high pressures [46] within accessible computer simulation time scales and shows a "nose-shaped" curve of temperature versus crystallization time [46], a feature found in experimental data on water solutions [51].

In our simulations, \( N = 512 \) water molecules are confined between two smooth planar walls, as shown schematically in Fig. 1. The walls are located at \( z_w = \pm 0.55 \) nm (wall-wall separation of 1.1 nm), which results in \( \approx 2 \) to 3 layers of water molecules. Periodic boundary conditions are used in the \( x \) and \( y \) directions, parallel to the walls.

We study two different forms of purely repulsive water-wall interaction. The first uses only the \( r^9 \) repulsive core, which we call the \( 1/r^9 \) repulsive potential, with the 512 water molecules confined between two walls perpendicular to the \( z \)-direction. Note that the confining plates are located along the \( z \)-direction and are separated by 2 to 3 molecular layers of water.

$$\phi(z) = 4\varepsilon_{OW} \left( \frac{\sigma_{OW}}{|z - z_{W}|} \right)^9 \quad \text{if} \quad |z - z_{W}| \leq 3^{1/6} \sigma_{OW},$$

$$\phi(z) = 0 \quad \text{if} \quad |z - z_{W}| > 3^{1/6} \sigma_{OW},$$

where \( \varepsilon_{OW} = 1.25 \) kJ/mol and \( \sigma_{OW} = 0.25 \) nm. For the \( 1/r^9 \) repulsive potential, we perform simulations for 56 state points, corresponding to seven temperatures \( T = 220, 230, 240, 250, 260, 280, \) and \( 300 \) K, and eight "geometric densities" \( \rho_g = 0.60, 0.655, 0.709, 0.764, 0.818, 0.873, 0.927, \) and \( 0.981 \) g/cm\(^3\), the same as studied in Ref. [24]. The geometric values of density do not take into account the fact that the repulsive interactions of molecules with the walls given by Eq. (1) increase the overall amount of available space relative to the LJ potential used in Ref. [24], since the \( \varepsilon_{OW} \) parameter of the \( 1/r^9 \) repulsive potential is smaller than the \( \varepsilon_{OW} \) used for the LJ confined system. For systems confined by LJ interactions, there is a well-defined preferred distance from the wall, making it relatively straightforward to evaluate the "effective" density of molecules confined by the attractive wall. In our system with only repulsive interactions, there is no such preferred distance, as emphasized by Fig. 2.
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We can approximate the effective density by examining the local density \( \rho(z) \) (Fig. 3). We utilize the fact that \( \rho(z) \) has an inflection, and estimate the effective \( L_z \) by the location where the second derivative of \( \rho(z) = 0 \), or where the first derivative of \( \rho(z) \) has a maximum. We must also add to this value of \( L_z \), the molecular diameter of water (0.278 nm) to calculate the real space available along the \( z \)-direction. The resulting “effective densities” for the \( 1/r^9 \) repulsive potential are \( \rho = 0.715, 0.777, 0.829, 0.890, 0.949, 1.000, 1.060, \) and \( 1.115 \) g/cm\(^3\). We will use these effective densities throughout the paper, since they will be more comparable to the effective densities with LJ confinement.

For the WCA-like repulsive potential, we perform simulations for 32 state points, corresponding to eight different temperatures and four different “geometric densities,” 0.60, 0.655, 0.709, and, 0.764 g/cm\(^3\), respectively. These geometric densities correspond to “effective densities” 0.80, 0.88, 0.95, and 1.02 g/cm\(^3\), respectively. Note that these effective densities were calculated using the method described in [24,31].

We control the temperature using the Berendsen thermostat with a time constant of 5 ps [52] and use a simulation time step of 1 fs, just as in the bulk system [46]. Water-water interactions are truncated at a distance 0.9 nm as discussed in Ref. [43].

III. THERMODYNAMICS AND STRUCTURE

One of the defining characteristics of water is the existence of a temperature of maximum density (TMD). Relative to bulk water, LJ confinement shifts the locus of the TMD to lower \( T \) by \( \approx 40 \) K [24]. Additionally, the sharpness of the density maximum is markedly decreased in comparison to the bulk. Figure 4 shows isotherms of \( P \) for LJ confinement, \( 1/r^9 \) repulsive confinement, and WCA-like repulsive confinement, for similar densities. A TMD in this plot is coincident with the minimum in the isochore. For \( 1/r^9 \) repulsive confinement, the minimum is very weak, but the location of the flatness in the isochore is near that of the system with LJ confinement. This result suggests the \( 1/r^9 \) repulsive confinement further suppresses the structural ordering of the molecules that is known to be responsible to the presence of a...
density maximum. The TMD for the case of WCA-like repulsive confinement again appears at the same $T$ as the $1/r^9$ repulsive confinement and LJ confinement cases but the iso-
chore in the TMD region is flatter than for the case of LJ confinement. Hence both kinds of the repulsive confinement suppress the structural ordering in lateral directions compared to the case of bulk and LJ confinement. We further notice that the value of the lateral pressure $P_l$ in the case of the LJ confinement approaches the value of $P_l$ in the case of WCA-like repulsive confinement at high temperatures. This behavior of $P_l$ for LJ confinement should be expected since at very high temperatures the molecules will not feel the potential minimum of the water-wall interaction.

In order to compare the structural properties of repulsive confinement with those of LJ confinement, we calculate the lateral oxygen-oxygen radial distribution function (RDF) defined by

\[ g_\parallel(r) = \frac{1}{\rho^2 V} \sum_{i \neq j} \delta(r - r_{ij}) \left[ \theta\left(z_i - z_j - \frac{\delta z}{2}\right) - \theta\left(z_i - z_j + \frac{\delta z}{2}\right) \right]. \]

Here $V$ is the volume, $r_{ij}$ is the distance parallel to the walls between molecules $i$ and $j$, $z_i$ is the $z$-coordinate of the oxygen atom of molecule $i$, and $\delta(x)$ is the Dirac delta function.

The Heaviside functions, $\theta(x)$, restrict the sum to a pair of oxygen atoms of molecules located in the same slab of thickness $\delta z=0.1$ nm. The physical interpretation of $g_\parallel(r)$ is that $g_\parallel(r)2\pi r dr \delta z$ is proportional to the probability of finding an oxygen atom in a slab of thickness $\delta z$ at a distance $r$ (parallel to the walls) from a randomly chosen oxygen atom. In a bulk liquid, this would be identical to $g(r)$, the standard RDF.

Figure 5 shows the temperature and density dependence of the lateral oxygen-oxygen pair correlation function for both $1/r^9$ repulsive [Figs. 5(a) and 5(b)] and WCA-like repulsive [Figs. 5(c) and 5(d)] confinements. For both repulsive confinements, the qualitative behavior of the dependence of $g_\parallel$ is the same. At low temperature and low density, the first two peaks in $g_\parallel$ appear at $r=2.78$ and $4.5$ Å, but at high densities the second peak moves to a larger distance. This behavior is nearly identical to that observed for water confined between LJ surfaces, and is discussed in detail in Ref. [24].

We also confirm the structural similarity with LJ confinement by calculating the lateral static structure factor $S_l(q)$, defined as the Fourier transform of the lateral RDF $g_\parallel(r)$,

\[ S_l(q) = \frac{1}{N} \sum_{j,k} \langle \exp(iq \cdot (r_j - r_k)) \rangle. \]

Here the $q$ is the corresponding wave vector in the $xy$ plane and $r$ is the projection of the position vector on the $xy$ plane.
In Fig. 6, we show the temperature and pressure dependence of lateral structure factors for both repulsive confinements. For both forms of repulsive confinement, the temperature and density dependence of $S(q)$ is similar. We find that confined water has a weaker prepeak at $q \approx 18 \text{ nm}^{-1}$ compared to bulk water [Fig. 7]. Consistent with the possibility that the local tetrahedrality is weakened by repulsive confinement. Of the three forms of confinement, the $S(q)$ for LJ confinement is most like bulk water [Fig. 7]. Local tetrahedrality becomes weaker in the case of repulsive confinements compared to LJ confinement. Further, we see that water in $1/r^9$ repulsive confinement is less structured in lateral directions compared to water in WCA-like repulsive confinement, indicated by a weaker peak at $q \approx 18 \text{ nm}^{-1}$ in $S(q)$ [Fig. 7].

IV. FREEZING OF TIP5P WATER

Bulk TIP5P water crystallizes within the simulation time for $\rho \approx 1.15 \text{ g/cm}^3$ at low temperatures [46]. Crystallization of confined water is seen in some simulations [3,7,24]. A similar crystallization appears in simulations when an electric field is applied in lateral directions to a system of water confined between silica walls [23].

At a plate separation of 1.1 nm with hydrophobic LJ confinement, water crystallizes to trilayer ice [24]. From our simulations of TIP5P water in repulsive confinements with the same plate separation of 1.1 nm, we find that the system does not freeze within accessible simulation time scales for $1/r^9$ repulsive confinement; however, the system freezes for WCA-like repulsive confinement. As a more stringent con-
firmation of this fact, we also use a starting ice configuration obtained from simulations with LJ confinement for the same thickness, and confirm that the ice melts to a liquid with \(1/r^9\) repulsive confinement. In Fig. 8, we show the evolution of potential energy and lateral structure factor with time, when the crystal formed in LJ confinement is kept between the \(1/r^9\) repulsive walls. The potential energy first increases and then reaches its equilibrium value of the liquid state accompanied by a structural change from a crystal (presence of sharp Bragg peaks) to a liquid (absence of Bragg peaks).

Based on this observation, it is tempting to claim that repulsion inhibits crystallization, and that a preferable distance from the walls determined by the attractive portion of the LJ potential is necessary to induce crystallization. However, as discussed above for the same plate separation 1.1 nm, \(1/r^9\) repulsive confinement with the chosen parameters increases the available space for molecules relative to LJ confinement. Hence to properly compare the crystallization behavior, we must adjust the separation of the wall so that the available space for the water molecules is the same in both systems. We can make the available space the same by tuning the separation of the plates or by tuning the potential. By tuning the parameters (see Fig. 2), where the values of parameter \(\sigma_{\text{OW}}\) and \(\varepsilon_{\text{OW}}\) for the modified \(1/r^9\)-repulsive potential are 1.25 kJ/mol and 0.23 nm, respectively, of the \(1/r^9\) repulsive potential in such a way such that the density profile along the \(z\)-axis becomes similar to the profile in the LJ confinement, we have identical values of the available space between the plates (see Fig. 9).

We find that for the repulsively confined systems, the crystal will also spontaneously form if the available space for molecules relative to plate separation—since the separation determines the accessible packing arrangements between the plates. Similar sensitivity to plate separation for monolayer ice was seen in Ref. [23].

In addition to examining the stability of initially crystalline structures, we also consider whether freezing from the liquid state occurs when we have the same effective plate separation. We find that for the repulsively confined systems, the crystal will also spontaneously form if the available space between the plates is the same as that for which initially crystalline configurations are stable (see Fig. 10). Hence plate separation appears to be the dominant cause in determining whether or not a crystal will form.

V. CONCLUSION

We have investigated the effects of two forms of purely repulsive water-wall interactions (repulsive confinement) on liquid thermodynamics and freezing of water between two parallel smooth plates. We compared our results with water in hydrophobic LJ confinement and found that thermody-

\[\text{FIG. 8. (a) A plot of potential energy changes for a crystal which had been previously formed in LJ confinement [24] and is now held in a } 1/r^9 \text{ repulsive confinement. (b) The crystal structure indicated by the sharp Bragg peaks melts, and (c) transforms, at a later time of about 1000 ps, into a liquid (indicated by the absence of Bragg peaks).}\]

\[\text{FIG. 9. (Color online) Density profile } \rho(z) \text{ of water along the } z \text{-direction for different potentials at the same geometric density. The repulsive confinement system freezes spontaneously when the parameters of the potential are modified such that the effective } L_z \text{ calculated from the } \rho(z) \text{ (red dotted line) for the repulsive system is the same as that for the LJ system (blue-dashed line) (see Fig. 2).}\]

\[\text{FIG. 10. (a) Potential energy as a function of time } t, \text{ for } 1/r^9 \text{ repulsive confinement when the effective } L_z \text{ is the same as the effective } L_z \text{ for LJ confinement at } T=260 \text{ K and geometric density } \rho_0=0.981 \text{ g/cm}^3. \text{ The confined water spontaneously freezes, indicated by the drop in potential energy. (b) The structure factor of the ice such formed resembles the trilayer ice seen in the case of LJ confinement [7,24].}\]
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dynamic, dynamic, and structural properties are qualitatively similar in all the cases. In other words, the properties of the liquid are only weakly dependent on the details of the confining potential for the specific case of smooth walls. Since all of these potentials disfavor water structure, one might call them hydrophobic, even when there is wall attraction. The most important parameter for this class of potentials is the plate separation, clearly demonstrated by the dependence of the freezing on the effective space between them. The fact that the liquid properties are only weakly sensitive to the details of the confining potential supports the idea that much can be learned about bulk water by examining confined water. This is critical for experimental studies since confinement is an effective tool to suppress crystal nucleation [12,15,18]. However, in many experimental situations the confining potential may be more complex; further computational work examining the role of surface structure and hydrophilic interactions that promote water structure will be valuable.

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[34] C. Rhykerd, M. Schoen, D. Diester, and J. Cushman, Nature
Two positive point charges of charge $q_H = 0.241e$ (where $e$ is the fundamental unit of charge) are located on each hydrogen atom at a distance 0.09572 nm from the oxygen atom; together they form an HOH angle of 104.52°. Two negative point charges $q_e = -q_H$ representing the lone pair of electrons are located at a distance 0.07 nm from the oxygen atom. These negative point charges are located in a plane perpendicular to the HOH plane and form an angle of $\cos^{-1}(1/3) = 109.47°$, the tetrahedral angle. To prevent overlap of molecules, a fifth interaction site is located on the oxygen atom, and is represented by a LJ potential with parameters $\sigma_{OO} = 0.312$ nm and $\epsilon_{OO} = 0.6694$ kJ/mol.